

النموذج (ب)

①

1-

(b) 15



2-

(c) $(x-2)^2 + (y+3)^2 + (z-4)^2 = 16$



3-

(b) $z = 5$



4-

$$\text{a) } \vec{BA} = \vec{A} - \vec{B} = (-1, -2, -3)$$

$$\vec{BC} = \vec{C} - \vec{B} = (-1, 4, 0)$$

$$\text{(i) } \cos(\angle ABC) = \frac{\vec{BA} \cdot \vec{BC}}{\|\vec{BA}\| \|\vec{BC}\|}$$

$$= \frac{(-1, -2, -3) \cdot (-1, 4, 0)}{\sqrt{1+4+9} \sqrt{1+16+0}}$$

$$= \frac{1-8+0}{\sqrt{14} \sqrt{17}} = \frac{-7}{\sqrt{14} \sqrt{17}}$$

$$\therefore m(\angle ABC) \approx 117^\circ$$

$$\text{(ii) } \therefore \vec{BC} = \vec{C} - \vec{B} \Rightarrow \vec{C} = \vec{BC} + \vec{B}$$

$$\vec{C} = (-1, 4, 0) + (3, 5, 4) = (2, 9, 4)$$

$$\vec{AC} = \vec{C} - \vec{A} = (0, 6, 3)$$

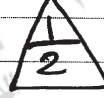
Die Richtungskomponente $= \left(\frac{\vec{AC} \cdot \vec{AB}}{\|\vec{AB}\|^2} \right) \cdot \vec{AB}$

$$= \frac{(0, 6, 3) \cdot (1, 2, 3)}{1+4+9} \cdot (1, 2, 3)$$

$$= \frac{0+12+9}{14} \cdot (1, 2, 3) = \left(\frac{3}{2}, 3, \frac{9}{2} \right)$$

Das Volumen des Parallelepipeds

$$= | \vec{A} \cdot \vec{B} \times \vec{C} |$$



$$= \begin{vmatrix} 1 & 4 & 2 \\ -3 & 2 & 1 \\ -1 & 1 & 4 \end{vmatrix}$$



$$= 1(7) - 4(-11) + 2(-1) = 49$$

(ii) Die Basisfläche = $\| \vec{A} \times \vec{B} \|$

$$\therefore \vec{A} \times \vec{B} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & 4 & 2 \\ -3 & 2 & 1 \end{vmatrix} = -7\vec{j} + 14\vec{k}$$

$$\therefore \| \vec{A} \times \vec{B} \| = \sqrt{(-7)^2 + (14)^2} = 7\sqrt{5}$$



Die Basisfläche = $7\sqrt{5}$

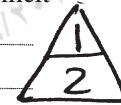
Flächeneinheit

Die Höhe des Parallelepipeds = $\frac{\text{Volumen}}{\text{Basisfläche}}$

$$= \frac{49}{7\sqrt{5}} = \frac{7\sqrt{5}}{5}$$

Längeneinheit

$$\approx 3.13 \text{ Längeneinheit}$$



(تراعى الحلول الأخرى)

5-

(b) 15



6-

(a) 10



7-

(b) 2



8-

$$\begin{array}{ccc|ccc} 1 & 1 & 1 & & & \\ a & b & c & & C_2 - C_1 & \\ a^2 & b^2 & c^2 & & C_3 - C_1 & \Rightarrow \end{array}$$

$$= \begin{array}{ccc|ccc} 1 & 0 & 0 & & & \\ a & b-a & c-a & & & \\ a^2 & b^2-a^2 & c^2-a^2 & & & \end{array} \begin{array}{c} \triangle \\ 1 \end{array}$$

$$= \begin{array}{ccc|ccc} 1 & 0 & 0 & & & \\ a & (b-a) & (c-a) & & & \\ a^2 & (b-a)(b+a) & (c-a)(c+a) & & & \end{array} \begin{array}{c} \triangle \\ \frac{1}{2} \end{array}$$

$$= (b-a)(c-a) \begin{array}{ccc|ccc} 1 & 0 & 0 & & & \\ a & 1 & 1 & & & \\ a^2 & b+a & c+a & & & \end{array} \begin{array}{c} \triangle \\ \frac{1}{2} \end{array} \begin{array}{c} C_3 - C_2 \\ \Rightarrow \end{array}$$

$$= (b-a)(c-a) \begin{array}{ccc|ccc} 1 & 0 & 0 & & & \\ a & 1 & 0 & & & \\ a^2 & b+a & c-b & & & \end{array} \begin{array}{c} \triangle \\ \frac{1}{2} \end{array}$$

$$= (b-a)(c-a)(c-b) \begin{array}{c} \triangle \\ \frac{1}{2} \end{array}$$

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9-

(d) π



10-

(c) $\tan \theta$

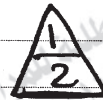


11-

Angenommen:

x^4 be T_{r+1}

$$T_{r+1} = {}^{12}C_r \left(\frac{-1}{x^2}\right)^r (x^2)^{12-r}$$



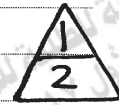
$$= {}^{12}C_r (-1)^r x^{24-4r}$$



$$24 - 4r = 4 \Rightarrow r = 5$$

\therefore der Term mit

x^4 is T_6



$$T_6 = {}^{12}C_5 (-1)^5 (x^4) = -792x^4$$

• die Ordnung des mittleren Term ist

$$\therefore \frac{12}{2} + 1 = 7$$

$$T_7 = {}^{12}C_6 \times \left(\frac{-1}{x^2}\right)^6 \times (x^2)^6 = {}^{12}C_6 = 924$$



\therefore Koeff. von

$$\frac{T_6}{T_7} = \frac{-792}{924} = \frac{-6}{7}$$



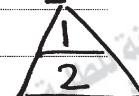
Koeff. von

$$\frac{\text{Koeff. von } T_6}{\text{Koeff. von } T_7} = \frac{r}{n-r+1} \times \frac{1^{\text{st}}}{2^{\text{nd}}}$$

$$= \frac{6}{12-6+1} \times \frac{1}{-1}$$



$$= \frac{-6}{7}$$



12-

$$\vec{n} \cdot \vec{r} = \vec{n} \cdot \vec{A}$$

$$(4, 10, -7) \cdot \vec{r} = (4, 10, -7) \cdot (2, -1, 0)$$

$$(4, 10, -7) \cdot \vec{r} = -2$$

$$4(x-2) + 10(y+1) - 7z = 0$$

$$4x + 10y - 7z + 2 = 0$$

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13-

(b) $(1, 1)$ 

14-

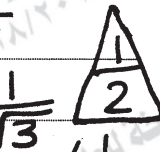
Die Gerade bildet gleiche Winkel mit den positiven Richtungen der Koordinatenachsen

$$\therefore \cos \theta_x = \cos \theta_y = \cos \theta_z$$

$$\therefore \cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1$$

$$\therefore \cos^2 \theta_x = \cos^2 \theta_y = \cos^2 \theta_z = \frac{1}{3}$$

$$\therefore \cos \theta_x = \cos \theta_y = \cos \theta_z = \pm \frac{1}{\sqrt{3}}$$



Der Richtungsvektor der Geraden Die vektorielle Form Die parametrischen

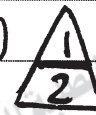
Gleichungen Die kartesische Gleichung

$$= (1, 1, 1)$$

$$= \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} \right)$$

$$\therefore \vec{r} = (3, 2, -1) + t \left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}} \right)$$

$$\therefore r = (3, 2, -1) + t (1, 1, 1)$$



$$\bullet x = 3 + t, y = 2 + t, z = -1 + t$$

$$x = 3 + \frac{1}{\sqrt{3}}t, y = 2 + \frac{1}{\sqrt{3}}t, z = -1 + \frac{1}{\sqrt{3}}t$$



$$\bullet x - 3 = y - 2 = z + 1$$

$$\frac{x-3}{\left(\frac{1}{\sqrt{3}}\right)} = \frac{y-2}{\left(\frac{1}{\sqrt{3}}\right)} = \frac{z+1}{\left(\frac{1}{\sqrt{3}}\right)}$$



$$\begin{pmatrix} 0 & -3 & 2 \\ 5 & 1 & 0 \\ 1 & -2 & -1 \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 7 \\ 4 \\ 1 \end{pmatrix}$$

$$AX = B$$

$$|A| = \begin{vmatrix} 0 & -3 & 2 \\ 5 & 1 & 0 \\ 1 & -2 & -1 \end{vmatrix} = 3(-5) + 2(-11) = -37 \neq 0$$

$$\text{Adj}(A) = \begin{pmatrix} -1 & 5 & -11 \\ -7 & -2 & -3 \\ -2 & 10 & 15 \end{pmatrix}^t = \begin{pmatrix} -1 & -7 & -2 \\ 5 & -2 & 10 \\ -11 & -3 & 15 \end{pmatrix}$$

$$A^{-1} = \frac{1}{|A|} \text{Adj}(A)$$

$$\therefore A^{-1} = \frac{1}{-37} \begin{pmatrix} -1 & -7 & -2 \\ 5 & -2 & 10 \\ -11 & -3 & 15 \end{pmatrix}$$

$$\therefore \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \frac{1}{-37} \begin{pmatrix} -1 & -7 & -2 \\ 5 & -2 & 10 \\ -11 & -3 & 15 \end{pmatrix} \begin{pmatrix} 7 \\ 4 \\ 1 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \frac{-1}{37} \begin{pmatrix} -37 \\ 37 \\ -74 \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \\ 2 \end{pmatrix}$$

$$\therefore x = 1, y = -1, z = 2$$

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النموذج (ب)

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16-

$$(b) {}^3C_1 \times {}^9C_3$$



17-

$$(b) 2 \cos \theta$$



18-

$$(d) \vec{r} = (2, 1, -3) + k(-1, 1, -2)$$



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19-

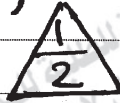
$$\textcircled{a} \quad Z = \frac{8(\sqrt{3}+i)}{(\sqrt{3}-i)} \times \frac{\sqrt{3}+i}{\sqrt{3}+i}$$

$$Z = \frac{8(3+2\sqrt{3}i-1)}{4}$$



$$Z = 8 \left(\frac{1}{2} + \frac{\sqrt{3}}{2} i \right) = 8 \left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right)$$

$$Z = 8 e^{\frac{\pi}{3}i}$$



$$\sqrt[3]{Z} = 2 e^{\frac{\pi+2\pi n}{3}i}, \quad i = 0, 1, -1$$



$$n=0 \quad \therefore \sqrt[3]{Z} = 2 e^{\frac{\pi}{9}i}$$



$$n=1 \quad \therefore \sqrt[3]{Z} = 2 e^{\frac{7\pi}{9}i}$$



$$n=-1 \quad \therefore \sqrt[3]{Z} = 2 e^{-\frac{5\pi}{9}i}$$



$$\textcircled{b} \quad (x+yi)(1-3i) = 37 \left(\frac{7+4\omega^2+3-4\omega^2}{(3-4\omega^2)(7+4\omega^2)} \right)$$



$$= 37 \left(\frac{10}{(3-4\omega^2)(7+4\omega^2)} \right)$$

$$= 37 \left(\frac{10}{21-16\omega^2-16\omega} \right)$$



$$= 37 \left(\frac{10}{21-16(\omega^2+\omega)} \right) = \frac{370}{37} = 10$$



$$\therefore x+yi = \frac{10}{1-3i} \times \frac{1+3i}{1+3i} = \frac{10(1+3i)}{10}$$



$$x+yi = 1+3i \quad \Rightarrow \quad x=1 \quad \text{und} \quad y=3$$



(تراجعى الحلول الأخرى)

(انتهت الإجابة وتراجعى الحلول الأخرى)