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Advances in Political Economy

Institutions, Modelling and Empirical Analysis

This book presents latest research in the field of Political Economy, dealing with the integration of economics and politics and the way institutions affect social decisions. The focus is on innovative topics such as an institutional analysis based on case studies; the influence of activists on political decisions; new techniques for analyzing elections, involving game theory and empirical methods.

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139 A deeper concern is that preferences may not be representable by weighted Euclidean utility functions: indifference curves may have shapes that are not elliptical. Weighted Euclidean utilities represent a particular class of convex preferences. 140
141
142 Preferences are (strictly) convex if the upper contour set defined by each indifference curve is (strictly) convex; that is, if the set of policies preferable to policy x is convex, for any x . Representable (strictly) convex preferences are representable 143
144 by (strictly) quasiconcave utility functions. If preferences are not strictly convex, 145
146 they cannot be represented by Euclidean utility functions, neither unweighted nor 147
148 weighted ones. The curvature imposed by Euclidean utilities is simply not adequate to represent the preferences.

149 An alternative assumption to Euclidean preferences is city-block preferences, 150
151 which define square indifference curves (with squares tilted at a 45 degree angle 152
153 relative to the axes of coordinates), and are representable by utility functions that are 154
155 decreasing in the l_1 distance $\|x - x^*\|_1 = \sum_{k=1}^K |x_k - x_k^*|$, where x_k is the policy 156
157 on issue $k \in \{1, \dots, K\}$. That is, agents with city block preferences calculate the 158
159 distance between two points by adding up the distance dimension by dimension, as 160
161 if traveling on a grid (that is why the l_1 or city block distance is sometimes called 162
163 “Manhattan distance”), and they prefer points closer to their ideal according to this 164
165 notion of distance. If preferences are city block, their utility representation is not 166
167 strictly quasiconcave, and it is not differentiable. Classic results on the instability 168
169 of simple majority rule (Plott 1967; McKelvey 1976) do not apply if agents have 170
171 city block preferences. In fact, the core of simple majority rule is not empty under 172
173 more general conditions if agents have city-block preferences (Rae and Taylor 1971; 174
175 Wendell and Thorson 1974; McKelvey and Wendell 1976; Humphreys and Laver 176
177 2009).

178 Humphreys and Laver (2009) invoke results from psychology and cognitive sciences (Shepard 1987; Arabie 1991) to argue that agents measure distance to objects with separable attributes by adding up the distance in each attribute, which implies that if the object under consideration is a policy bundle on separable issues, agents measure distance according to the city block function. 179
180

181 Grynviski and Corrigan (2006) find that a model that assumes voters have city block preferences provides a better fit of vote choice in US presidential elections than an alternative model that assumes voters have linear Euclidean preferences. 182
183 Westholm (1997) finds that a model with city block preferences outperforms a model with quadratic Euclidean preferences, when aiming to predict vote choice in Norwegian elections. However, a binary comparison between city block utilities based on the l_1 metric $\|x - x^*\|_1 = \sum_{k=1}^K |x_k - x_k^*|$ and the linear Euclidean utilities based on the l_2 metric $\|x - x^*\|_2 = (\sum_{k=1}^K (x_k - x_k^*)^2)^{\frac{1}{2}}$ is unnecessarily restrictive: 184
185 l_1 and l_2 are special cases of the Minkowski (1886) family of metric functions, which parameterized by δ , gives the distance between x and x^* as:

$$\|x - x^*\|_\delta = \left(\sum_{k=1}^K (x_k - x_k^*)^\delta \right)^{\frac{1}{\delta}}. \quad (1)$$

Rather than comparing $\delta = 1$ (linear city block) and $\delta = 2$ (linear Euclidean), it appears more fruitful to estimate parameter δ . Rivero (2011) estimates δ for several Spanish regional elections and finds that $\hat{\delta} \in (0.92, 1.17)$; none of the estimates is significantly different from $\delta = 1$, and they are all significantly different from $\delta = 2$. These tests support the use of linear city block over linear Euclidean utility functions.

Utility functions that are linearly decreasing in expression (1) are not additively separable unless $\delta = 1$. To satisfy additive separability, the utility function must be linearly decreasing in the δ power of $\|x - x^*\|_\delta$, so that

$$u(x, x^*) = - \sum_{k=1}^K (x_k - x_k^*)^\delta, \quad (2)$$

with linear city block utilities corresponding to $\delta = 1$, and quadratic Euclidean to $\delta = 2$. Notice that any parameter $\delta > 1$ results in strictly convex preferences and strictly quasiconcave and differentiable utility functions, while $\delta < 1$ results on preferences that are not convex, and utility functions that are neither strictly quasiconcave, nor differentiable. Ye et al. (2011) estimate parameter δ using the utility function (2) and voting data from the American National Election Studies corresponding to the 2000, 2004 and 2008 Presidential elections. However, their results are inconclusive, obtaining estimates that vary greatly across elections and, most puzzlingly, across candidates.

Further empirical work appears necessary to establish which utility functions provide a better fit, and whether the standard assumption of convex preferences is justified.

Most of the literature, and all of the discussion above, considers the set of alternatives as exogenously given: there is a subset $X \subseteq \mathbb{R}^K$ that is given, and agents have preferences over X . In this view, the question on the adequate assumption on the shape of the utility functions (Euclidean, city block, Minkowski with parameter δ) is a question on what primitive preferences over alternatives do we believe that agents have on $X \subseteq \mathbb{R}^K$.

However, the spatial representation of the set of feasible policies is itself a representation used for convenience, just as the utility functions are representations of underlying preferences. If, for instance, there are three policies x , y and z and agent i prefers x to y to z , and agent i is indifferent between y and a fair lottery between x and z , then we can map the three policies to the real line using a mapping $f : \{x, y, z\} \rightarrow \mathbb{R}$ such that $f(x) = 0$, $f(y) = 0.5$ and $f(z) = 1$ and then we can say that the agent has a linear utility function over $[0, 1]$ with ideal point at 0. But we can represent the same underlying preferences using a mapping $g : \{x, y, z\} \rightarrow \mathbb{R}$ such that $g(x) = 0$, $g(y) = \sqrt{\frac{1}{2}}$ and $g(z) = 1$ and say that the agent has a quadratic utility function over $[0, 1]$ with ideal point at 0. Under this perspective, we see that the shape of the utility function is an object of choice for the theorist who wishes to study an individual: using a different mapping of the set of alternatives into a vector space leads to indifference curves of different shapes. The spatial representation of

the set of alternatives and the utility function we use in this space jointly determine the assumptions we make on the underlying preferences of the agent.

Once we recognize that the spatial representation of the set of alternatives is an endogenous choice made by the theorist who wishes to model preferences, we can ask new questions: can all preferences over policies be represented by Euclidean utility functions *in some space*? if not, what preferences can be represented by Euclidean utility functions? If we accept a spatial representation with great dimensionality, we obtain a positive result: any preference profile with N agents can be represented by utility functions that are Euclidean for all N agents if we let the mapping of the set of alternatives X into \mathbb{R}^K contain $K \geq N$ dimensions (Bogomolnaia and Laslier 2007). If we care for the number of dimensions in our spatial representation, we do not obtain such a positive result. Suppose the policy issues are exogenously given, and we want to use no more than one dimension per issue in our spatial representation. In this case, while we can represent any single-peaked, separable preference relation of a single individual using quadratic Euclidean utility functions over an appropriately chosen spatial representation of the set of alternatives, we cannot represent the preferences of all N individuals with quadratic Euclidean utility functions in any spatial representation unless the underlying preference profile satisfies very restrictive conditions (Eguia 2011a).³

For any single-peaked preference profile with separable preferences, we can map the set of alternatives into \mathbb{R}^K so as to represent the preferences of a given agent by quasiconcave utility functions over the chosen map. However, depending on the preference profile, any mapping that achieves this may be such that the utility representations of the preferences of other agents violate quasiconcavity and/or differentiability. Whether preference profiles in any given application are such that the preferences of all agents can be represented in some map with quasiconcave utility functions is an open empirical question.

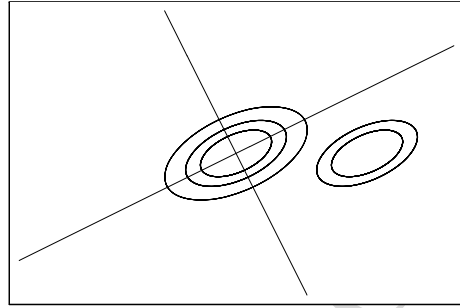
4 Concerns About Separability of Preferences

Expressions (1) or (2) above, or variations with weights for each dimension, allow us to relax the assumption that indifference curves have circular or elliptical curvature. We are free to assume any degree of curvature, including preferences that are not convex by choosing $\delta < 1$. These generalizations of the standard model from $\delta = 2$ to any $\delta > 0$ preserve the assumption that preferences are separable across issues: ordinal preferences over alternatives on a given issue do not depend on the realized outcome on other issues.

Milyo (2000b) and (2000a) notes that preferences over multiple dimensions of public spending cannot possibly be separable. Suppose a fixed unit of national income is to be allocated between public spending on policy one, public spending on

³Calvo et al. (2012) analyze an additional complication: agents may not agree on which alternative is to the right or left of another on a given issue. If so, we cannot use a unique spatial representation; rather, we must have subjective maps of the set of the set of alternatives, one for each agent.

Fig. 1 Obtaining separability
by using a new basis of
vectors



policy two, and private consumption. Decreasing marginal utility over consumption of public goods means that as public spending on policy one increases, the opportunity cost of spending on issue two also increases, so the ideal of expenditures on issue two must decrease with the amount spent on issue one. Preferences over public spending on issues one and two cannot be separable. This problem is easily solved by redefining the policy dimensions over which we assume that agents have separable preferences: let the first dimension be total public spending, and let the second dimension be the fraction of public spending devoted to issue one. Preferences may well be separable under this representation of the set of issues, and in any case they escape Milyo's (2000b) and (2000a) critique.

A more insidious difficulty arises if preferences are truly non-separable, not due to budgetary concerns, but because agents' ideal values on a given issue actually depend on the outcomes on other issues. For instance, it is possible that agents have non-separable preferences about immigration policy and the social safety net, preferring a more generous safety net if immigration policy is restrictive so redistributive policies benefit only natives, than if immigration policy is lax so redistributive policies would in part favor immigrants. Lacy (2001a,b, 2012) uncovers evidence of such non-separability across various pairs of issues.

If agents have non-separable preferences, but the correlation between issues is the same for all agents, then the problem is addressed by considering new, endogenous policy dimensions over which agents have separable preferences. Suppose that there are two complementary issues, such that for any agent i ,

$$u(x_1, x_2) = -(x_1 - x_1^i)^2 - (x_2 - x_2^i)^2 + (x_1 - x_1^i)(x_2 - x_2^i).$$

These utility functions, depicted for two arbitrary agents in Fig. 1, are not separable over the two issues. However, if we use a different basis of vectors, as depicted in Fig. 1, and consider the new two dimensional vector space given by the two tilted axes of coordinates in Fig. 1, then agents have separable preferences over the new, endogenous dimensions.

This solution fails if agents have non-separable preferences and the correlation between preferences on different issues is heterogeneous across agents. In this case, we cannot create dimensions to make all agents separable over our newly defined dimensions. For instance, returning to non-separability between immigration and

323 social safety net, if some agents prefer a larger safety net to help needy immigrants
 324 when immigration policy is lax, while other agents prefer a smaller safety net to not
 325 spend money on immigrants when immigration policy is lax, then we can redraw
 326 the axes to make the preferences of one group of agents separable, but in doing
 327 so, the preferences of the other group of agents remain non-separable. In very non-
 328 technical terms, agents have non-separable preferences if their indifference curves
 329 are tilted; if all agents have curves equally tilted, we can tilt the whole map to return
 330 to a standard model over newly defined dimensions.

331 If, on the contrary, different agents have preferences tilted in different directions,
 332 we cannot correct this problem by tilting the whole map. We need instead to intro-
 333 duce parameters to accommodate the correlation across issues. This is a consider-
 334 able setback, similar to the problem of agents who assign different relative weights
 335 to the various dimensions –but more damaging, because we need more parameters
 336 to fix it. In order to accurately represent the preferences of agents who disagree on
 337 the weights they assign to the different dimensions we need to add one parameter
 338 per dimension per agent or group of agents who disagree on these weights, for a
 339 maximum of $(K - 1)(N - 1)$ new parameters if there are N agents and K dimen-
 340 sions. In order to represent the preferences of agents who disagree on the correlation
 341 in preferences between issues, we must add one correlation parameter per possible
 342 pair of issues and per agent or group of agents who disagree, for a maximum of
 343 $\frac{K(K-1)}{2}N$ new parameters.

344 While violations of separability do not affect classic results on the instability
 345 of simple majority rule as long as preferences are smooth (Plott 1967; McKelvey
 346 1979), they affect how we can interpret and use common spatial models. Consider
 347 the structured-induced equilibrium theory (Shepsle and Weingast 1981), which pro-
 348 poses that the instability is solved by choosing policy dimension by dimension. In
 349 the standard structured-induced equilibrium theory, the order in which the legisla-
 350 ture considers the various policy dimensions is irrelevant, because preferences are
 351 separable. With non-separable preferences, the order in which each policy dimen-
 352 sion is considered affects the chosen policy outcome. For a second example, con-
 353 sider the ideal point estimation literature (Poole and Rosenthal 1985; Clinton et al.
 354 2004): if preferences are not separable, estimating the ideal point of each legislator
 355 is not enough to predict vote choice.

358 5 Discussion

361 Theoretical and empirical work questions not only the standard assumption of Eu-
 362 clidean utility functions in multidimensional spatial models, but the more general
 363 assumptions of separable, convex and/or smooth preferences.

364 Standard spatial models suffer from limitations that I have not considered here.
 365 For instance, an increasing body of literature argues that we must add a candidate
 366 valence term to capture the actual preferences of voters about candidates. Valence
 367 is any quality that all voters agree is good, and makes the candidate who possesses
 368

369 more of it more attractive to all voters. Current research on valence seeks to endog-
 370 enize it and to analyze its relation to the candidate's spatial location (Ashworth and
 371 Bueno de Mesquita 2009; Zakharov 2009; Serra 2010 and 2012; Krasa and Polborn
 372 2010, 2012; or Schofield et al. 2011). In this chapter I analyze concerns about a
 373 basic pillar of the spatial model: the assumption that agents have preferences over
 374 a vector space that represents the set of feasible policies, preferences that can be
 375 represented by analytically convenient utility functions. Valence, dynamics, uncert-
 376 tainty, bounded rationality, other-regarding preferences or other improvements can
 377 be added to the basic spatial model to generate richer theories, but any theory with
 378 a spatial component must address the challenges posed in this chapter about the
 379 appropriate formalization of spatial preferences in the theory.

380 Further empirical work is necessary to establish whether agents have convex pref-
 381 erences over policy bundles with multiple policy issues. Assuming the functional
 382 form (1) or, if we want to satisfy additive separability, functional form (2) for the
 383 utility functions, empirical work must estimate parameter δ . If the estimated param-
 384 eter $\hat{\delta}$ is less than 1, the consequences for theoretical work are dramatic: Preferences
 385 are not convex, and hence utility functions are neither quasiconcave, nor differ-
 386 entiable. Standard results in the literature that rely on these assumptions, most notably
 387 the instability of majority rule (Plott 1967; McKelvey 1976; Schofield 1978), would
 388 not apply. Whereas, results that rely on city block preferences (Humphreys and
 389 Laver 2009) or on non-differentiable utility functions (Kamada and Kojima 2010)
 390 would become more relevant, and further theoretical work would be needed to es-
 391 tablish what results in the literature obtained under assumptions of quasiconcavity
 392 or differentiability of preferences are robust and apply in environments with agents
 393 whose preferences are not representable by quasiconcave or differentiable utility
 394 functions.

395 If the estimated parameter $\hat{\delta}$ is consistently greater than 1, even if it is not near 2,
 396 much of the theoretical literature will be validated. The main impact of obtaining a
 397 better estimate of δ in utility functions of the form (2) that is $\hat{\delta} \neq 2$ but $\hat{\delta} > 1$ will be
 398 to improve the fit of further empirical work on ideal point estimation models (Clint-
 399 on et al. 2004; Poole and Rosenthal 1985), or vote choice models, by assuming that
 400 agents have utility functions with the curvature corresponding to the best estimate
 401 of δ within the parameterized family of utility functions (2), instead of assuming
 402 that agents have utility functions with parameter $\delta = 2$ even though parameter $\delta = 2$
 403 provides a poorer fit for the model.

404 With regard to separability, violations of the assumption typically do not affect
 405 equilibrium existence or convergence results on models of electoral competition or
 406 policy choice. However, application of spatial models to specific real world poli-
 407 ties or electorates should take into account existence evidence on non-separability
 408 across various pairs of issues (Lacy 2001a,b, 2012), so that if the models explicitly
 409 include such issues, utility functions are not assumed to be separable over them.
 410 Many spatial models do not include many issues; rather, they collapse the list of all
 411 issues onto two dimensions, one that groups economic issues (from left/pro-state to
 412 right/pro-market) and another that includes all cultural issues (from left/progressive
 413 to right/conservative). It is more difficult to determine whether preferences are sep-
 414 arable or not over such dimensions, which are not precisely defined. Nevertheless, if

415 future empirical work reveals evidence of a systematic correlation between prefer-
 416 ences across economic and cultural issues, models should either seek to define new
 417 dimensions (new ways of bundling or weighing the issues) in such a way that prefer-
 418 ences are separable over the new dimensions, or else, if this cannot be achieved,
 419 then it may be necessary to allow for non-separable preferences, estimating not only
 420 an ideal point, but also a degree of correlation between dimensions for each agent
 421 or group of agents.

422 Euclidean preferences have been an extremely useful tool in the development of
 423 multidimensional spatial models that can explain electoral competition, government
 424 formation and legislative policy-making. Generalizations that show that several the-
 425 oretical results are robust if preferences are not Euclidean but are convex and smooth
 426 allowed us to conjecture that Euclidean preferences are only a simplifying shortcut
 427 with limited effect on our ability to understand the political processes we model.
 428 Nevertheless, we lack convincing empirical evidence that preferences are convex
 429 and smooth. If preferences are not convex and smooth, nor separable, and our the-
 430 oretical models assume that they are, we are impaired in our ability to understand
 431 and predict the political processes we study.

432 Future empirical work shall establish whether preferences are convex and
 433 smooth, and whether we can find systematic evidence of differentiated non-
 434 separability over pairs of issues, or systematic differences in the weights assigned
 435 to different dimensions, across different groups of voters or legislators. Future (bet-
 436 ter) theories must make assumptions that are consistent with these future empirical
 437 findings.
 438

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A Non-existence Theorem for Clientelism in Spatial Models

Daniel Kselman

1 Introduction

In spatial models of political competition, political parties typically announce positions on one or more issue dimensions; voters then choose from among these parties according to their preferences over the same issue dimensions. Put otherwise, spatial models typically analyze *programmatic* elections in which the link between voter choice and elite behavior is consummated indirectly, via collectively applicable policy issues.¹ In contrast, a growing body of research in comparative politics and comparative political-economy investigates *clientelistic* linkages between citizens and elected officials. Such linkages are grounded not in national-level public policy debates, but rather in a direct and contingent exchange of votes (or other forms of political participation...) for tangible material or professional rewards. These inducements take many forms: jobs in the public sector, access to the electric grid, washing machines, alcohol, fuel, etc. In such contexts, in addition to evaluating political parties' policy stances on one or more programmatic issues, voters choose based on parties' ability to provide targeted inducements.

A series of recent papers, reviewed in Sect. 2 below, has analyzed clientelism in a game theoretic setting. While all make valuable contributions to the literature on contingent electoral exchange, none explicitly introduces clientelistic concerns into the traditional spatial model, which has for decades been the work-horse in formal political theory. This paper develops a spatial model in which political parties strategically choose: (1) their programmatic policy position, (2) the effort they

¹A similar accountability mechanism underpins the 'Responsible Party Government' model, which dates at least to Lipset and Rokkan (1967), and sees ties between political parties and voters as grounded in campaign and governance strategies on issues of national-level public policy.

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47 devote to clientelism as opposed to the promotion of their programmatic position,
 48 and (3) the set of voters who are targeted to receive clientelistic benefits. Section 3
 49 presents the model's actors, their utility functions, and the actions which comprise
 50 their choice sets. Section 4 then demonstrates that, absent stronger restrictions on
 51 candidate behavior, there will never exist Nash Equilibria with positive clientelistic
 52 effort: given some clientelistic proposal by their opponent, candidates can always
 53 propose a slightly 'narrower' set of recipients and win an electoral plurality.

54 This is not to say that the game in its most general form is always character-
 55 ized by instability. On the contrary, if voter responsiveness to clientelistic resources
 56 is sufficiently low, then the game's Nash Equilibrium will be for all candidates to
 57 choose the median voter's ideal point, and to devote 100 % of their campaign effort
 58 to promoting this platform. Thus, the game in its most general form yields either
 59 traditional median voter convergence or theoretical instability. Section 5 relates this
 60 general result to past literature on instability in coalition formation processes. It also
 61 discusses a set of necessary conditions for the emergence of Nash Equilibria with
 62 positive levels of clientelism. One condition is that parties have differential abilities
 63 to target distinct subsets of voters. A second condition is that political parties face
 64 a *binding turnout constraint*. When turnout is not a given and parties have differ-
 65 ential abilities to target distinct subsets of voters, the need to balance one's interest in
 66 courting the electoral median with that in maintaining the support of one's ideologi-
 67 cal base leads, at times, to the adoption of positive equilibrium levels of clientelism.
 68

70 2 Theories of Clientelism

71 So as to highlight this paper's specific contributions, here I briefly outline recent
 72 theoretical research on the causes of clientelism. In the Introduction to their edited
 73 volume, Kitschelt and Wilkinson (2007) present an argument to explain the mix
 74 of clientelistic and programmatic appeals in politicians' vote production functions.
 75 Driving this mix is the interaction between economic development and electoral
 76 competitiveness.² At low levels of economic development politics is heavily client-
 77 telistic, and increasingly so as competitiveness increases. At high levels of economic
 78 development, politics is heavily programmatic and increasingly so as competitive-
 79 ness increases. Finally, it is at intermediate levels of development that politicians
 80 invest more equitably in both forms of linkage. To complement these basic compar-
 81 ative statics, the authors also highlight the role of a publicly controlled political-
 82 economy and formal political institutions in conditioning the mix of linkage strate-
 83 gies.
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 88 ²Competitiveness is a notably tricky concept to precisely define and operationalize. Different au-
 89 thors have assigned the concept different empirical referents. Kitschelt and Wilkinson (2007) de-
 90 fine competitive elections as those in which "... elections are close between rival blocs of parties...
 91 and there is a market of uncommitted voters sufficiently large to tip the balance in favor of one or
 92 another bloc." (p. 28)