

Artificial Intelligence

Lab 5

Informed Search

Agenda

Uninformed vs. informed search

What is Informed Search?

Informed Search

- Heuristic Functions
- A^*

Uninformed vs. informed search

- **Uninformed search** (BFS, UCS, DFS)
 - Knows the actual path cost $g(s)$ from start to a node s in the fringe, but that's it.



- **Informed search**



- Also, has a heuristic value $h(s)$ that represents the **cost** from start node to goal node. ('h' = heuristic, non-negative)
- Can be **much faster** than uninformed search.

Informed Search (Heuristic Search)

- Most informed search algorithms include as a component of $f(n)$ a **heuristic function**.
 - $h(n)$ is the **estimated** cost of the cheapest path from the state at node n to a **goal state**.
 - heuristic function are arbitrary, nonnegative, problem specific functions, with one constraint:
 - If n is goal node, then $h(\text{goal}) = 0$
- **For Example**, a **heuristic** is a **function** tells us **approximately** how far the **current state** is from the **goal state** (i.e. **smaller numbers are better**).

Heuristic information in search = Hints

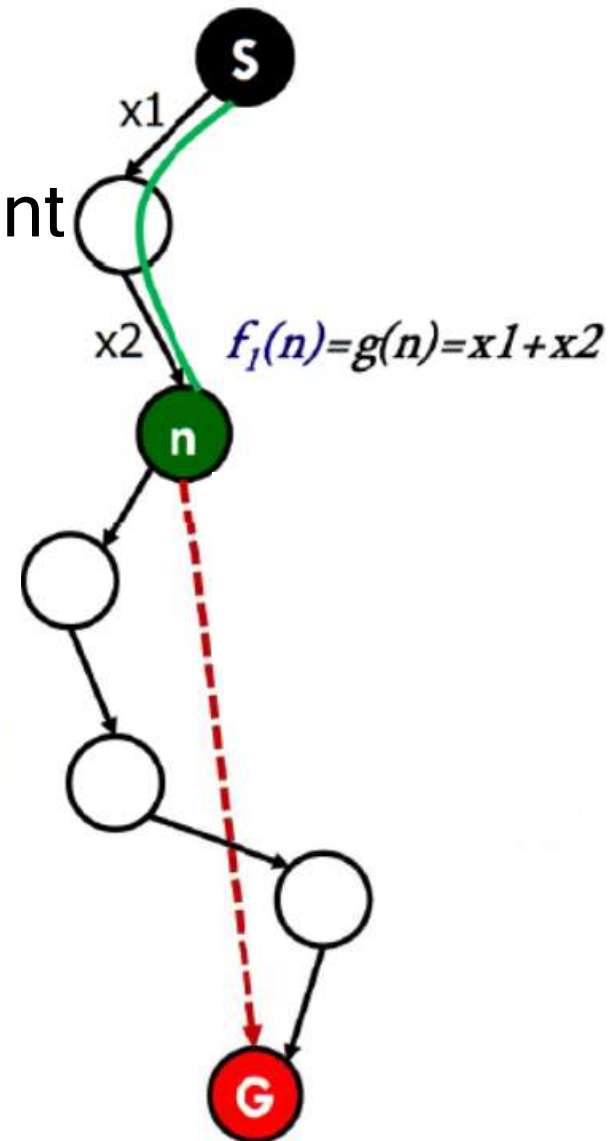
Heuristic Functions

There are 3 approaches to define $f(n)$:

1. $f(n)$ measures the value of the current state (its “goodness” “distance”)

$$f_1(n) = g(n)$$

similar to the uniform cost search (UCS)
where $g(n)$ is the cost to get to n (*from initial state*)



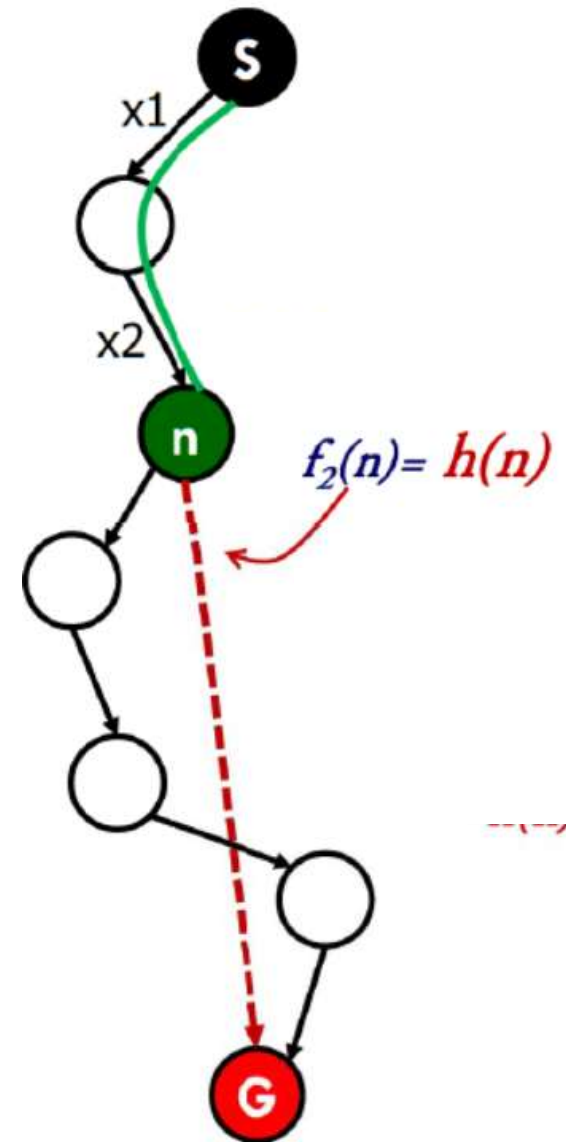
Heuristic Functions

There are 3 approaches to define $f(n)$:

2. $f(n)$ measures the estimated **cost** of getting to the goal from the current state:

$$f_2(n) = h(n)$$

where $h(n)$ is the estimate of the cost to get from n to a goal

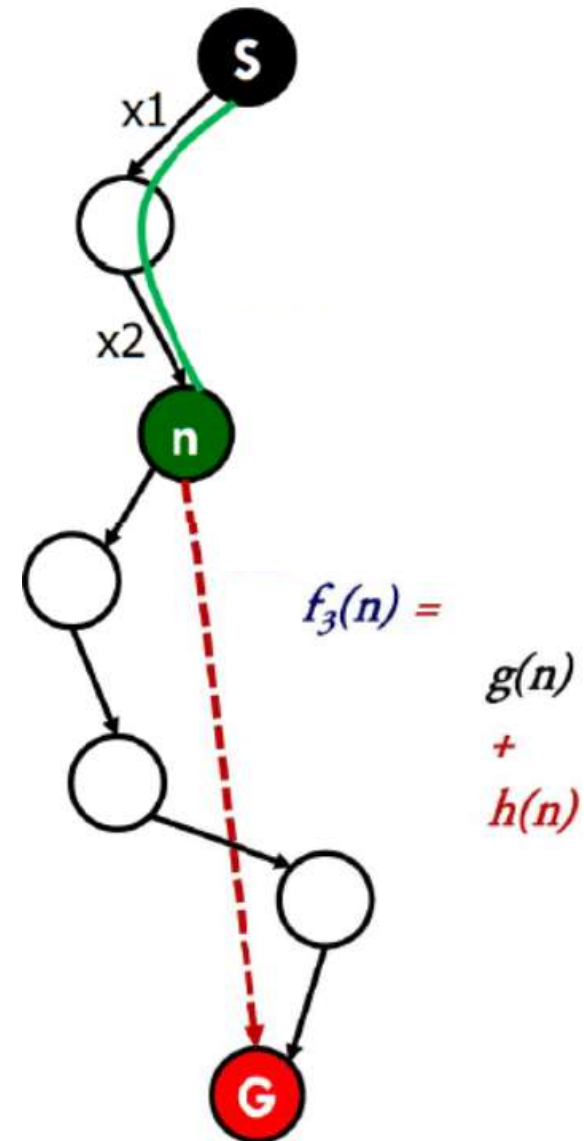


Heuristic Functions

There are 3 approaches to define $f(n)$:

3. $f(n)$ measures the **estimated cost** of getting to the goal from the **current state** and the cost to get to n from the initial state.

$$f_3(n) = g(n) + h(n)$$



Informed Search - A*

- Greedy Search minimizes a heuristic $h(n)$ which is an estimated cost from a node n to the goal state. it is **neither optimal nor complete**.
- Uniform Cost Search minimizes the cost $g(n)$ from the initial state to n . UCS is **optimal and complete** but **not efficient**.
- **New Strategy**: Combine Greedy Search and UCS to get an **efficient** algorithm which is **complete and optimal** ... **A*** algorithm.

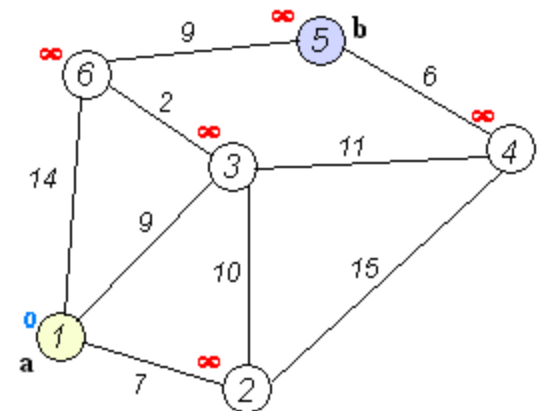
Using Heuristics in A*

- A* uses a heuristic function which combines $g(n)$ and $h(n)$: $f(n) = g(n) + h(n)$.
- $g(n)$ is the exact cost to reach node n from the initial state (cost so far up to node n).
- $h(n)$ is an **estimation** of the remaining cost to **reach** the **goal**.
- $f(n)$ is the estimated **total cost** of path through n to goal

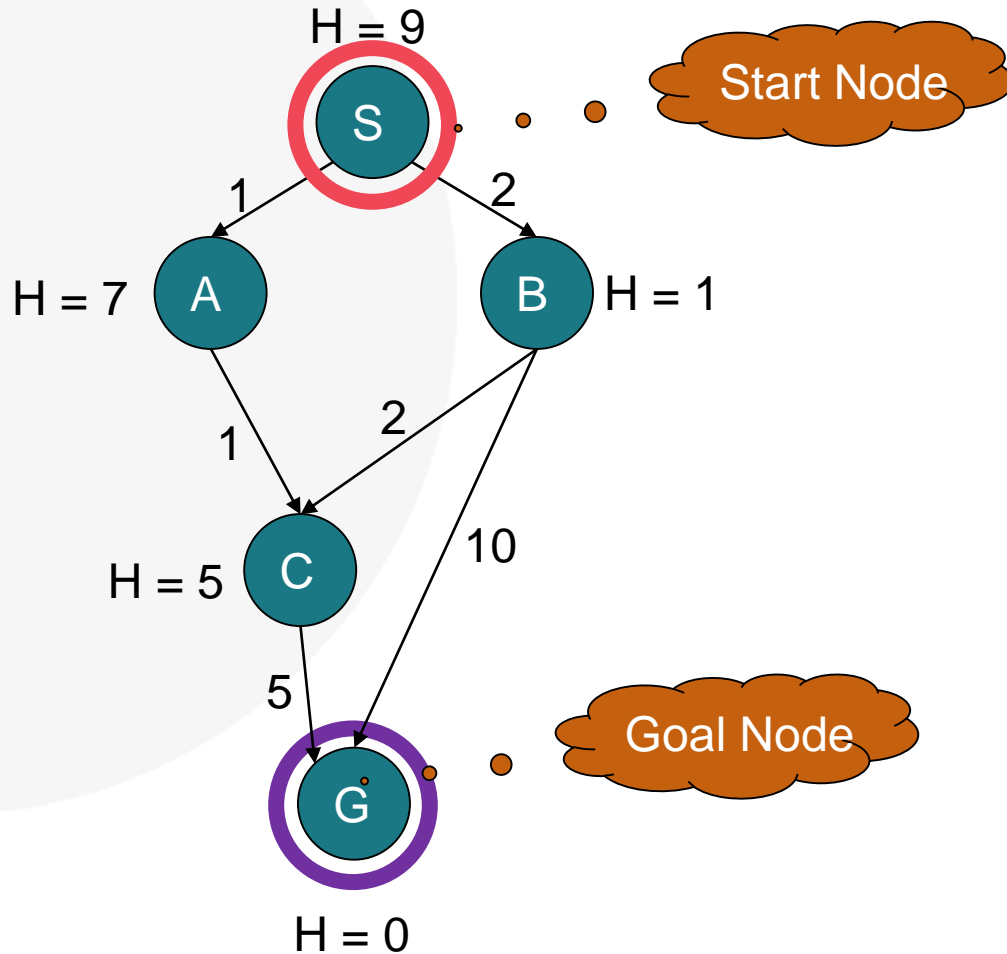
Informed Search – A*

Algorithm A star:

1. Put the start node **S** on the list called **OPEN** and empty list for **CLOSED**
2. If **OPEN** is empty, exit with failure
3. Remove from **OPEN** and place on **CLOSED** a node **n** for which **f(n)** is minimum
4. If **n** is a goal node, exit (trace back pointers from **n** to **S**)
5. Expand **n**, generating all its successors and attach to them pointers back to **n**.
For each successor **n'** of **n**
 1. If **n'** is not on **OPEN**, estimate $h(n')$, $g(n') = \text{totalOldCost}(S \rightarrow n')$, $f(n') = g(n') + h(n')$, and place it on **OPEN** and sort **OPEN** Ascending.
 2. If **n'** is already on **OPEN**, then check if $h(n')$ is lower for the new version of **n'**. If so, then update $h(n')$ with lower value.
 3. If $g(n')$ is not lower for the new version, do nothing.
6. Goto 2.



Informed Search – A*



Opened	Closed
{9S}	{}
{3B,8A}	{9S}
{8A, 9C,12G}	{9S, 3B}
{7C, 12G}	{9S, 3B,8A}
{7G}	{9S, 3B,8A, 7C}
	{9S, 3B,8A, 7C, 7G}

Traversed Path:

{S, A, C, G}
With cost = 7

Example – Puzzle 8 Game

- Given an initial state of the board, the combinatorial search problem is to find a sequence of moves that transitions this state to the goal state
- The **blank space** is going to be represented with the number 0.
- The **blank space** may be swapped with a component in one of the four directions {'Up', 'Down', 'Left', 'Right'}, one move at a time

Initial state =

2	8	3
1	6	4
7		5

Goal State =

1	2	3
8		4
7	6	5

Heuristic Measures the Cost to the Goal

- Assuming that **moving** one tile in any direction will have **1** unit cost.
- A state X would be better than a state Y if the estimated cost of getting from X to the goal is lower than that of Y
 - because X would be closer to the goal than Y
- **8-Puzzle heuristic Function:**
There are two ways of calculations with ignoring blank node:

h1: The **number** of **misplaced** tiles.

h2: The **sum** of the distances of the tiles from their **goal** positions. By calculating how far the tile from its goal position is to sum the **number of horizontal and vertical** positions.

Calculating Heuristic

5	4	
6	1	8
7	3	2

Current State

1	2	3
8		4
7	6	5

Goal State

Using H1:

$$H(\text{Initial State}) = 7$$

Using H2:

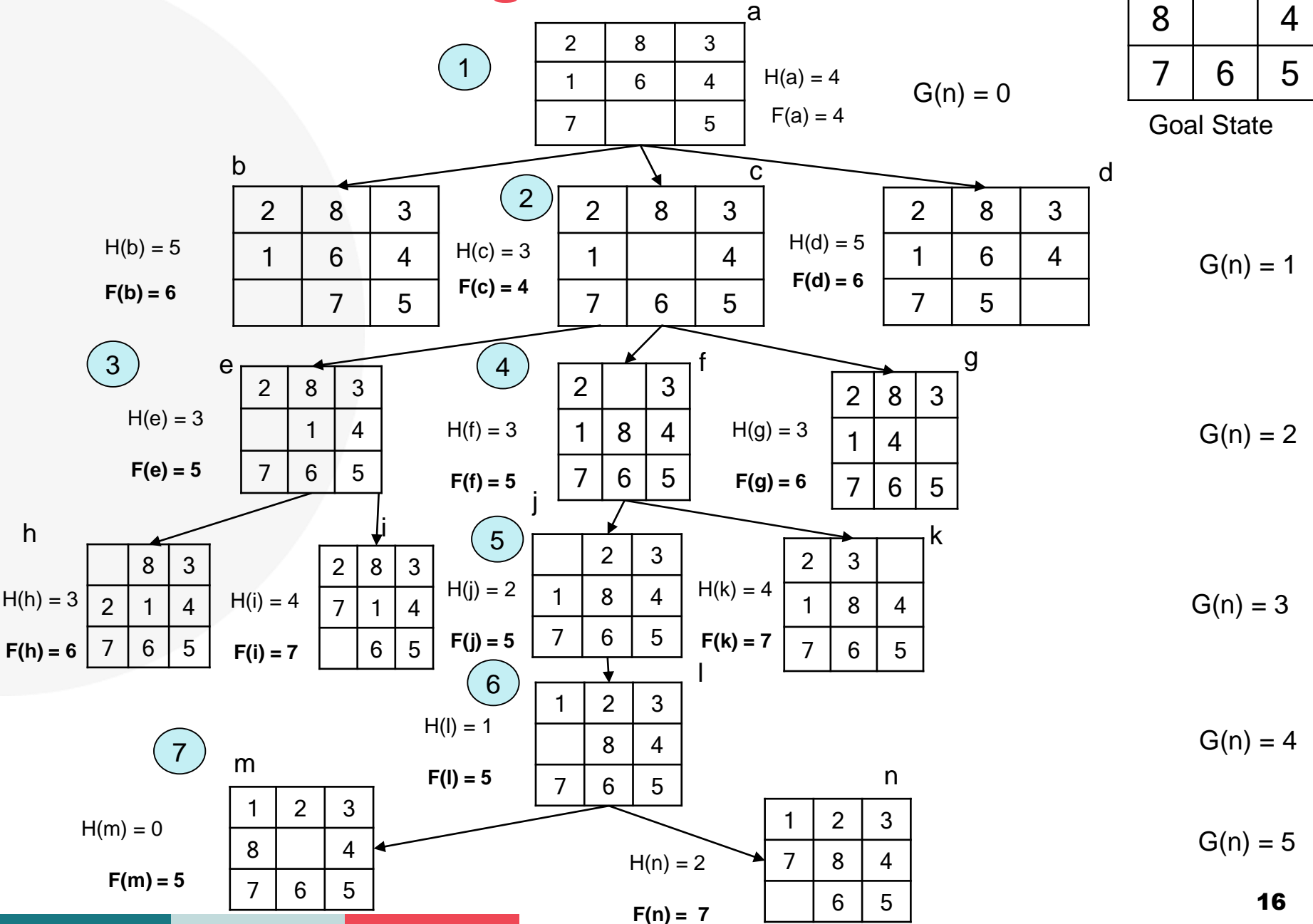
$$H(\text{Initial State}) = 2 + 3 + 3 + 2 + 4 + 2 + 0 + 2 = 18$$

2 represents how many steps does 1 need to be in his goal position.

8 Puzzle Game – Using A* + H1

1	2	3
8		4
7	6	5

Goal State



Milestone

Milestone 2 will include search algorithms (BFS, DFS, UCS and A*).

It will be announced on course-sites.



Questions?